

1. Data set information: $n = 275$ cow and sheep yogurts were tested for the presence of some microorganisms. Variable that was observed: Ph
2. Sturges rule for number of bins in histogram
 $k = \lceil \log_2 n + 1 \rceil$, $\lceil \cdot \rceil$ denotes the ceiling of a number (next integer)
3. density function in R. Different options for the parameter bw (bandwidth):
 - a. `bw = "nrd"`
 As presented in class. Under this selection

$$h_{\text{opt}} = 1.059 \tilde{s} n^{-1/5}, \tilde{s} = \min \left\{ \frac{\text{IQR}}{1.345}, s \right\}.$$
 To find this value type `bw.nrd(x)`, with x denoting the data.
 - b. `bw = "nrd0"`
 Similar to what we presented in class. It uses a different multiplier to cover a wider range of distributions (not only normal); see Silverman's book page 48

$$h_{\text{opt}} = 0.9 \tilde{s} n^{-1/5}, \tilde{s} = \min \left\{ \frac{\text{IQR}}{1.345}, s \right\}.$$
 To find this value type `bw.nrd0(x)`, with x denoting the data.
This is the default choice in R.
 - c. `bw = "ucv"`
 Uses unbiased cross validation to find h_{opt} .
 To find this value type `bw.ucv(x)`, with x denoting the data.
 For more info check for example <https://bookdown.org/egarpor/NP-UC3M/kde-i-bwd.html#kde-i-bwd-cv>
 - d. `bw = "bcv"`
 Uses biased cross validation to find h_{opt} .
 To find this value type `bw.ucv(x)`, with x denoting the data.
 For more info check for example <https://bookdown.org/egarpor/NP-UC3M/kde-i-bwd.html#kde-i-bwd-cv>
 - e. `bw = "SJ"`
 Uses the idea from Sheather and Jones (1991): find pilot estimates of the derivatives involved.
 To find this value type `bw.SJ(x)`, with x denoting the data.
4. density function in R. The number of equally spaced points (argument n is the function) at which the density is to be estimated. The default is 512 x 's, from (from argument) $\min(\text{data}) - 3h$ (the default value) to (to argument) $\max(\text{data}) + 3h$ (the default value), where data denoting the available data, that based on we wish to perform the density estimation, and h is the bandwidth that we use in the function. The value 3 above is the default value of the `cut` argument.

5. `ksmooth` function in R. Uses `n.points = max(100, length(x))` for estimating the function (`x` denotes the explanatory variables data) and the function is evaluated in `x.points` that are chosen in such a way to uniformly cover the range of `x`.